EELS: recent developments and new perspectives

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EELS in the TEM: recent developments and new perspectives

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Outline

- Introduction: EELS in the TEM
- Core losses
- Low losses
- Even lower losses
- Conclusion



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The constituent of the TEM



The objective lens





STEM & STEM-EELS

- The electron beam is formed as as focused probe scanned on the sample
- The signal is acquired on the detectors pixel by pixel
- The focused probe is a convergent electron beam. The bright field and Dark field detectors are radially symmetric
- The convergence semi-angle of the probe is called α. Typicall 10-30 mrad
- EELS is acquired in the hole of the DF detector (retracting the BF one). Collection angle is <= convergence in general.



Instrumentation



Excitation process for EELS







Outline



- Core losses
- Low losses
- Even lower losses
- Conclusior



Core losses



Relevant quantity: scattering crosssection as a function of angle q and energy loss E.

It is given for one atom.

We consider a transition from initial state | I > to final state | F > for the core electron of the atom

q: momentum transfer



Theory of core losses

transition from core (occupied) to unoccupied state We need quantum mechanics! System = fast incoming electron + target electron first order perturbation theory First Born approximation perturbation potential is Coulomb potential



H.A.Bethe: 1930:

Zur Theorie des Durchgangs schneller Korpuskularstrahlen durch Materie

Annalen der Physik, vol. 397, Issue 3, pp.325-400

Theory of core loss

Transition probability per unit time dP_{if} from an initial state $|i\rangle$ to a final state $|f\rangle$ situated between ν_f and $\nu_f + d\nu_f$.

$$dP_{if} = \frac{2\pi}{\hbar} |\langle f | V | i \rangle|^2 d\nu_f \,\delta(E_i - E_f)$$

Initial and final state of the system :

$$ert i
angle = ert ec k
angle \otimes ert I
angle$$

and
 $ert f
angle = ert ec k'
angle \otimes ert F
angle$

 $|I\rangle$ and $|F\rangle$ Initial and final states of the target electron.

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Theory of core loss

 \vec{k} before the interaction \vec{k}' after.

$$\vec{q} = \vec{k} - \vec{k}'$$

$$dP_{if} = \frac{2\pi}{\hbar} |\langle F| \otimes \langle \vec{k}' | V | \vec{k} \rangle \otimes |I\rangle|^2 d\nu_f \delta(E_I - E_F + E)$$

 $\langle \vec{k}' | V | \vec{k} \rangle$? ? $\longrightarrow V$ Coulomb potential

$$\langle \vec{k}' | V | \vec{k} \rangle = \frac{1}{4\pi\epsilon_0} \int (2\pi)^{-3} d^3 r \frac{e^2}{|\vec{r} - \vec{R}|} e^{i(\vec{k} - \vec{k}')\vec{R}}$$

 \vec{r} position vector of the fast electron \vec{R} of the target electron

Theory of core loss



Theory of core loss

$$d\sigma = \sum_{i,f} rac{dP_{if}}{j_0}$$

 j_0 current density of the plane wave

$$\psi_{\vec{k}}(\vec{R}) = (2\pi)^{-3/2} e^{i\vec{k}.\vec{R}}$$
 $j_0 = (\hbar k) / ((2\pi)^3 m)$

$$d\sigma = \sum_{I,F} \frac{me^4}{(\hbar 2\pi\varepsilon_0)^2 q^4 k} |\langle F|e^{i\vec{q}\cdot\vec{R}}|I\rangle|^2 d\nu_f \delta(E_I - E_F + E)$$

 $d\nu_{f} = d\nu_{t} \, d\nu_{e} \, (d\nu_{t} : \text{target electron}, \, d\nu_{e} : \text{fast electron})$ $d\nu_{e} = (k'm) / \hbar^{2} dEd\Omega$

Theory of core loss

If the final state is expressed in an orthogonal basis set : $d\nu_t=1$

$$d
u_f = k' rac{m}{\hbar^2} dE d\Omega$$

 $\frac{\partial^2 \sigma}{\partial E \partial \Omega} = \sum_{I,F} 4 \frac{m^2 e^4}{\hbar^4 (4\pi)^2 \varepsilon_0^2 q^4} \frac{k}{k'} |\langle F| e^{i\vec{q}.\vec{R}} |I\rangle|^2 \delta(E_I - E_F + E)$

Relativistic effects : $m
ightarrow \gamma m$

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Introduction

$$\frac{\partial^2 \sigma}{\partial E \partial \Omega} = \sum_{I,F} \frac{4\gamma^2}{a_0^2 q^4} \frac{k'}{k} |\langle F|e^{i\vec{q}.\vec{R}}|I\rangle|^2 \delta(E_I - E_F + E) = \frac{4\gamma^2}{a_0^2 q^4} \frac{k'}{k} S(\vec{q}, E)$$

$$S(\vec{q}, E) = \sum_{F} |\langle F|e^{i\vec{q}.\vec{R}}|I\rangle|^2 \delta(E_I - E_F + E)$$

S: Dynamic form factor

*a*₀ : Bohr radius

$$a_0 = rac{4\piarepsilon_0\hbar^2}{me^2}$$

 $ec{q} = ec{k} - ec{k'}$ $\gamma = (1 - ec{v^2}/ec{c^2})^{-1/2}$

R F Egerton, *Electron energy-loss spectroscopy in the TEM*, Rep. Prog. Phys. 72 (2009) 016502 (25pp); Egerton R F 1996 *Electron Energy-Loss Spectroscopy in the Electron Microscope* 2nd edn (New York: Plenum/Springer)

Introduction



Introduction Dipole approximation

Side approximation

$$S(\vec{q}, E) = \sum_{F} |\langle F|e^{i\vec{q}.\vec{R}}|I\rangle|^{2}\delta(E_{I} - E_{F} + E)$$
If $\vec{q}.\vec{R} \ll 1$ we can write $e^{i\vec{q}.\vec{R}} \simeq 1 + i\vec{q}.\vec{R}$
 $S(\vec{q}, E) = \sum_{F} |\langle F|i\vec{q}.\vec{R}|I\rangle|^{2}\delta(E_{I} - E_{F} + E)$
 $S(\vec{q}, E) \propto q^{2}$; $\frac{\partial^{2}\sigma}{\partial E\partial\Omega} \propto \frac{1}{q^{4}}S(\vec{q}, E)$
with the scattering geometry, $q^{2} = k^{2}(\vartheta_{E}^{2} + \vartheta^{2})$
Lorenzian distribution $\frac{\partial^{2}\sigma}{\partial E\partial\Omega} \propto \frac{1}{\vartheta^{2} + \vartheta_{e}^{2}}$





ELNES: Introduction







ELNES: anisotropy/relativity



Electric field of a moving charge is compressed in the direction of movement

Coulomb coupling becomes anisotropic Coupling with momentum transfer parallel to the electron's trajectory becomes smalle

Coupling with momentum transfers perpendicular to the electron's trajectory becomes larger

P. Schattschneider, C. Hébert, H. Franco, and B. Jouffrey. PRB, 72:045142–1 – 045142–8, 2005. Hébert & al. Ultramicroscopy 106 (2006) 1139



ELNES: anisotropy



Application: sp2/sp3 ratio

Nanocarbon as Robust Catalyst: Mechanistic Insight into Carbon-Mediated Catalysis**

Jian Zhang, Dangsheng Su,* Aihua Zhang, Di Wang, Robert Schlögl, and Cécile Hébert



Relativistic spectra Wien2k

- TELNES3 can calculate the DDSCS using any of three interaction potentials
- Nonrelativistic :

$$\frac{\partial^2 \sigma}{\partial E \partial \Omega} = \left[\frac{4\gamma^2 a_0^{-2}}{q^2}\right]^2 \frac{k_f}{k_i} \sum_{i,f} \left| \left\langle f \left| e^{i\boldsymbol{q}\cdot\boldsymbol{r}} \right| i \right\rangle \right|^2 \delta \left(E_f - E_i - E \right)$$

Relativistic :

$$\frac{\partial^2 \sigma}{\partial E \partial \Omega} = \left[\frac{4\gamma^2 a_0^{-2}}{q^2 - \left(\frac{E}{\hbar c}\right)^2} \right]^2 \frac{k_f}{k_i} \sum_{i,f} \left| \left\langle f \left| e^{iq.r} \left(1 - \frac{\mathbf{v}_{\theta} \cdot \mathbf{p}}{m_e c^2} \right) \right| i \right\rangle \right|^2 \delta \left(E_f - E_i - E \right) \right|$$

Relativistic small q (dipole) approximation :

$$\frac{\partial^2 \sigma}{\partial E \partial \Omega} = \left[\frac{4\gamma^2 a_0^{-2}}{q^2 - \left(\frac{E}{\hbar c}\right)^2} \right]^2 \frac{k_f}{k_i} \sum_{i,f} \left| \left\langle f \left| \tilde{\boldsymbol{q}} \cdot \boldsymbol{r} \right| i \right\rangle \right|^2 \delta \left(E_f - E_i - E \right) \right]$$

P. Schattschneider, C. Hébert, H. Franco, and B. Jouffrey. PRB, 72:045142–1 – 045142–8, 2005.

Relativistic spectra Wien2k

Graphite C K for 3 tilt angles. Beam energy 300 keV, collection angle = 2.4mrad.

Left: nonrelativistic calculation. Right: relativistic calculation.



White lines $S(\vec{q}, E) = \sum_{F} |\langle F|e^{i\vec{q}.\vec{R}}|I\rangle|^2 \delta(E_I - E_F + E)$ Final state: ??Initial state:
Core stateEasiest approximation: forget about crystal: atomic model• Orientation dependence of the EELS of graphitic material• White lines and their applications

ELNES: fine structure interpretation



ELNES: fine structure interpretation





ELNES: fine structure interpretation



Using white lines: reduction of NiO

Q. Jeangros, A Hessler-Wyser, Jan van Herle, Cécile Hébert

Anode synthesized as NiO-YSZ Reduction of NiO to Ni during 1st operation (activation)



Ni - current conductor & catalyst for H_2 oxidation YSZ – ionic conductor

Ni structure//chemistry after reduction at 700 °C inside ETEM



Using white lines: reduction of NiO



As-sintered NiO-YSZ anode

Phase distribution Yttria distributed inhomogenously → lonic conduction properties Gallium due to FIB

- < 1.5%at in bulk
- > 1.5% at on top of holes

Activated Ni-YSZ anode

Reduction at 700 °C inside ETEM Porous & inhomogenous Ni structure Ni nanoparticles

- → Reaction mechanisms
- \rightarrow Ni(OH)₂
- Artifact gallium oxide

500 nm





Using white lines: reduction of NiO









ELNES: fine structure



Kungliga Svenska Vetenskapsakademien har den 13 oktober 1998 beslutat att med det **NOBELPRIS** som detta år tillerkännes den som gjort den viktigaste-kemiska upptäckten eller förbättringen med ena hälften belönä **Walter Kohn** för hans utveckling av täthetsfunktionalteorin.



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ELNES: fine structure



ELNES: fine structure



Core Loss: theory





New developments

PRL 109, 246101 (2012)

PHYSICAL REVIEW LETTERS

week ending 14 DECEMBER 2012

Simulation of Spatially Resolved Electron Energy Loss Near-Edge Structure for Scanning Transmission Electron Microscopy

M. P. Prange,^{1,2,*} M. P. Oxley,^{1,2,†} M. Varela,² S. J. Pennycook,^{2,1} and S. T. Pantelides^{1,2,3}

¹Department of Physics and Astronomy, Vanderbilt University, Nashville, Tennessee 37235, USA ²Materials Science and Technology Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA ³Department of Electrical Engineering and Computer Science, Vanderbilt University, Nashville, Tennessee 37235, USA (Received 29 August 2012; revised manuscript received 9 November 2012; published 12 December 2012)

Aberration-corrected scanning transmission electron microscopy yields probe-position-dependent energy-loss near-edge structure (ELNES) measurements, potentially providing spatial mapping of the underlying electronic states. ELNES calculations, however, typically describe excitations by a plane wave traveling in vacuum, neglecting the interaction of the electron probe with the local electronic environment as it propagates through the specimen. Here, we report a methodology that combines a full electronicstructure calculation with propagation of a focused beam in a thin film. The results demonstrate that only a detailed calculation using this approach can provide quantitative agreement with observed variations in probe-position-dependent ELNES.

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New developments



FIG. 2 (color online). (a) Integrated experimental O K-shell intensity (top) and simultaneously acquired ADF signal (bottom). (b) A typical spectrum showing schematically the ΔE measurement. The line scan indicated on (a) is the same as that used in Fig. 4.







New developments

Microsc. Microanal. 20, 784-797, 2014 doi:10.1017/S1431927614000610

(a) integrated (b) 543.5 eV (c) 548.9 eV

0 1 2 3 4 5 6

Oxley & al. Simulation of Probe Position-Dependent Electron Energy-Loss Fine Structure

Oxygen K-shell ionization scattering potentials in STO for

- (a) the energy integrated potential,
- (b) (b) for Eloss = 543.5 eV
- and (c) Eloss = 548.9 eV,

(**d**) normalized diagonal intensity line scans as indicated by the cyan line shown on (**a**).

An energy broadening of 0.35 eV has been applied in all cases.



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Low Loss

SSD and loss function





Low Loss: the Kröger equation

The relation between the double differential cross section and the loss function is a "little bit" more complicated

$$\begin{aligned} \frac{\partial P(\omega, \mathbf{k}_{\perp})}{\partial \omega \partial^2 k_{\perp}} &= \frac{e^2}{\pi^2 \hbar v^2} \cdot \underbrace{\Im \left[\frac{\mu^2}{\epsilon \phi^2} \cdot D \right]}_{\mathbf{k}_{\perp}^{\mathbf{k}_{\perp}}} \text{Volume term} \\ &- \frac{2k_{\perp}^2 (\epsilon - \epsilon_0)^2}{\phi_0^4 \phi^4} \cdot \left\{ \frac{\phi_{01}^4}{\epsilon \epsilon_0} \left(\frac{\sin^2(\frac{\omega D}{2v})}{L^+} + \frac{\cos^2(\frac{\omega D}{2v})}{L^-} \right) \right. \\ &+ \beta^2 \cdot \frac{\lambda_0 \omega \phi_{01}^2}{\epsilon_0 v} \cdot \left(\frac{1}{L^+} - \frac{1}{L^-} \right) \cdot \sin\left(\frac{\omega D}{v}\right) \\ &- \beta^4 \cdot \frac{\omega^2}{v^2} \cdot \lambda_0 \lambda \left(\frac{\cos^2(\frac{\omega D}{2v}) tanh(\lambda D/2)}{L^+} + \frac{\sin^2(\frac{\omega D}{2v}) coth(\lambda D/2)}{L^-} \right) \right\} \end{aligned}$$

Following abbreviations were used:

$$\begin{split} \lambda &= \sqrt{k_{\perp}^2 - \frac{\epsilon \omega^2}{c^2}}, \quad \lambda_0 = \sqrt{k_{\perp}^2 - \frac{\epsilon_0 \omega^2}{c^2}}\\ L^+ &= \lambda_0 \epsilon + \lambda \epsilon_0 tanh(\lambda D/2), \quad L^- = \lambda_0 \epsilon + \lambda \epsilon_0 coth(\lambda D/2)\\ \beta^2 &= \frac{v^2}{c^2}, \quad \phi_{01}^2 = k_{\perp}^2 + \frac{\omega^2}{v^2} - (\epsilon + \epsilon_0) \frac{\omega^2}{c^2}\\ \phi^2 &= \lambda^2 + \frac{\omega^2}{v^2}, \quad \phi_0^2 = \lambda_0^2 + \frac{\omega^2}{v^2}\\ Z. \text{ Phys. 216 (1968), 115-135} \quad \mu^2 = 1 - \epsilon \beta^2, \quad \mu_0^2 = 1 - \epsilon_0 \beta^2 \end{split}$$

Low Loss

Relativistic effects in semiconductors - Bulk





Low Loss: some solutions

difference method (Si)



Low Loss





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High Energy Resn Monochrmtd EELS-STEM (HERMES)



30x improvement of EELS energy resolution!



High energy resolution ZLP acquired with HERMES





Phonon mapping with monochromated STEM EELS



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Challenges:

- High spatial **and** high energy resolution can only be achieved with a **Convergent probe** !
- Cs corrected STEM. Several 10 of mradians convergence. (1st diffraction @10).
- The incoming electron is everything but a plane wave...
- Geometry, thickness, orientation of the specimen matters

Conclusion

- Huge amount of information in ELNES
- No need for super-high energy resolution
- Already simple interpretation give lot of information
- Many ways to calculate ELNES
- · Still active field of development

TEM, EELS and simulation

